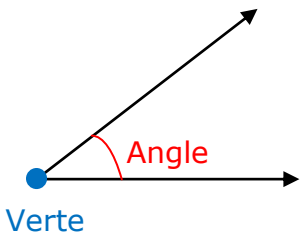
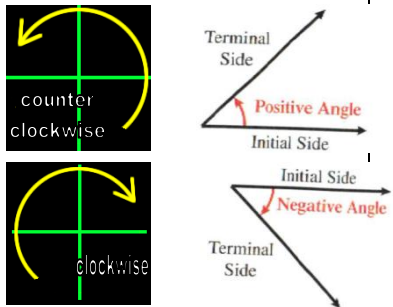

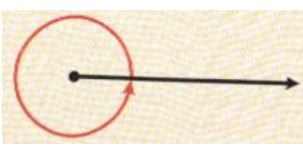
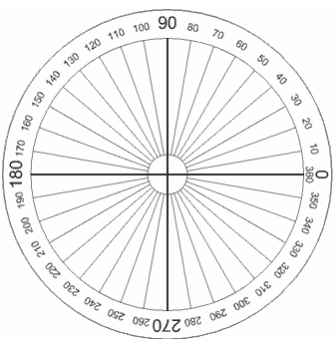
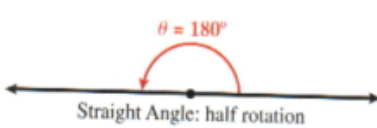
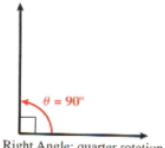


Notes #4-2: Angle Measure

| Word  | Definition  | Picture   |
|---|---|---|
| <b>Angle</b>  | Two rays share the same endpoint.<br>The common endpoint is called a vertex   |    |
| <p>We say an angle is formed when a ray is rotated around its endpoint.<br/>The ray in the original position is called the <b>initial ray</b> (assumed to be x-axis).<br/>The ray after it is rotated is called the <b>terminal ray</b>.<br/>Counterclockwise rotation = positive angle<br/>Clockwise rotation = negative angle</p> |   |    |
| <b>Degree measure</b>   | <p><a href="http://www.mathsisfun.com/geometry/degrees.html">http://www.mathsisfun.com/geometry/degrees.html</a></p>  <p style="text-align: right; font-size: 2em;">1°</p> <p style="text-align: center;">This is how large 1 Degree is</p> |   |
| <b>360°</b>   | An angle formed by one complete counterclockwise rotation   |  |
| <p style="text-align: center;">A full circle is 360°</p> <p><b>Why 360 degrees?</b> Probably because old calendars (such as the Persian Calendar) used 360 days for a year - when they watched the stars they saw them revolve around the North Star one degree per day.</p>  |   |  |
| <b>180° Straight Angle</b>  | Half Rotation   |  |
| <b>90° Right Angle</b>  | Quarter Rotation  |  |

If have a full schedule (8am-3:20pm), you are in school for 7.3 hours each day

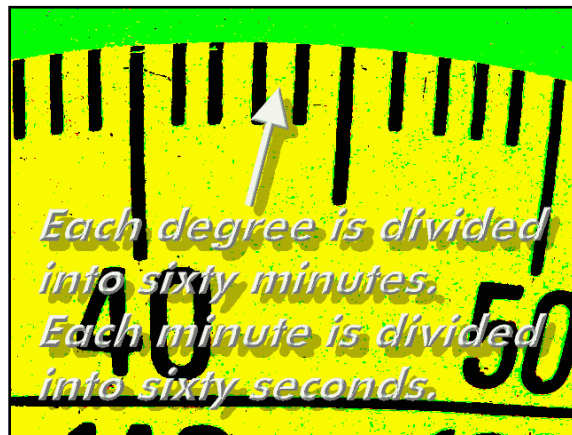
However, only 6.53 hours are devoted to academic endeavors.

Find the specific number of hours, minutes and seconds you spend perusing academic interests.

### Degree measurement works a lot like time ....

| Degree Measurements |                       |
|---------------------|-----------------------|
| Minutes             | 60 minutes = 1 degree |
| Seconds             | 60 seconds = 1 minute |

| Hour Measurement |                       |
|------------------|-----------------------|
| Minutes          | 60 minutes = 1 hour   |
| Seconds          | 60 seconds = 1 minute |



### Example 1: Converting between decimal and DMS and DMS to decimal

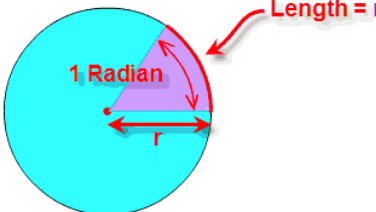
a. 102.75

b. 40.34722

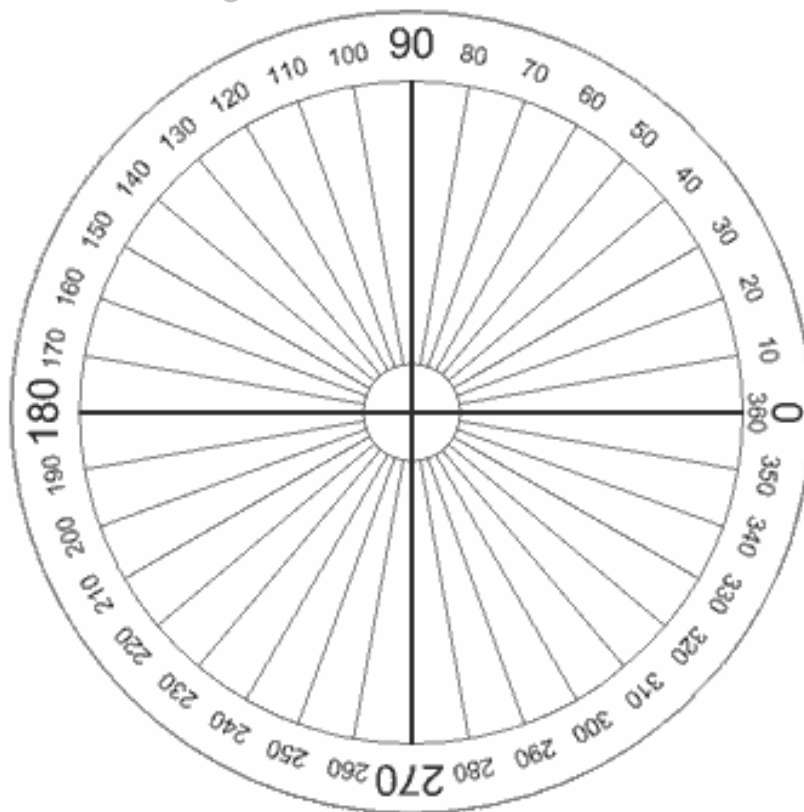
c.  $280^{\circ}10'$

d.  $17^{\circ}55'19''$

However, we can also use **radians** to measure angles!

|                              |   |   |
|------------------------------|---|---|
| <p><b>Radian measure</b></p> | <p>A radian is the angle made when we take the radius and wrap the radius around the edge of the circle</p> <p><a href="http://www.mathsisfun.com/geometry/radians.html">http://www.mathsisfun.com/geometry/radians.html</a></p> <p>Angle measures that do not have <math>^{\circ}</math> are assumed to always be in <b>radians!</b></p> |  |
|------------------------------|---|---|

## The degree-radian connection



Conversation Factor for Radians  $\leftrightarrow$  Degrees

**Example 2:** converting between radian and degree measure

Convert decimal into radian

Convert radian into DMS

a.  $\frac{\pi}{8}$

b.  $16 \text{ radians}$

c.  $61.8^\circ$

d.  $5^\circ 35'$

e.  $75^\circ 12' 24''$

f.  $\frac{24\pi}{9}$