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## LESSON <br> 5-4

## SSS Triangle Congruence

## Practice and Problem Solving: A/B

## Use principles of congruence to answer Problems 1-3.

1. Show that $\triangle B C D$ is congruent to $\triangle F G H$ if $x=6$.

2. In the figure, $\overline{A B} \cong \overline{A D}$. Explain how you know that $\angle B \cong \angle D$.
$\qquad$
$\qquad$
$\qquad$
3. In the figure, $H$ is equidistant from the endpoints of line segment $\overline{G J}$. Leon said that means that $\overrightarrow{H K}$ is the perpendicular bisector of $\overrightarrow{G J}$. Was he right? Explain your reasoning.

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Use the figure at the right for the two-column proof.
4. Point $O$ is the center of the circle. The chords $\overline{X Y}$ and $\overline{Z Y}$ are congruent. Fill in the missing statements and reasons to prove that $\angle X$ is congruent to $\angle Z$.

Given: Circle $O, \overline{X Y} \cong \overline{Z Y}$
Prove: $\angle X \cong \angle Z$

| Statements | Reasons |
| :--- | :--- |
| 1. $\overline{X Y} \cong \overline{Z Y}$ | 1. |
| 2. | 2. |
| 3. | 3. Reflexive property of congruence |
| 4. | 4. |
| 5. | 5. |


4. Possible answer:

| Statements | Reasons |
| :--- | :--- |
| 1. $\overline{G H} \cong \overline{K L}$ | 1. Given |
| 2. $\overline{G H} \\| \overline{K L}$ | 2. Given |
| 3. $\angle G H L \cong$ <br> $\angle K L H$ | 3. Opposite interior <br> angles of parallel <br> lines $\overline{G H}$ and $\overline{K L}$ <br> and transversal $\overline{J F}$ |
| 4. $\overline{F L} \cong \overline{J H}$ | 4. Given |
| 5. $F L+L H=F H$ <br> $=J H+L H$ <br> $=J L$ | 5. Segment addition <br> 6. $\overline{F L} \cong \overline{J L}$ |
| 6. Definition of <br> congruent <br> segments |  |
| $\triangle F G K L$ | 7. SAS Triangle <br> Theorem |

## Practice and Problem Solving: Modified

1. $\angle P$
2. $\angle R$
3. $\angle Q$
4. $\angle N \cong \angle M ; \overline{A F} \cong \overline{T B} ; \overline{A N} \cong \overline{T M}$
5. Possible answer: For the SAS Congruence Theorem to apply, the $34^{\circ}$ angle of each triangle must be included between two pairs of corresponding congruent sides.
6. $\angle A$ and $\angle T$
7. $\overline{F N}$ and $\overline{M B}$
8. 

$\left.\begin{array}{|c|l|}\hline \text { Statements } & \text { Reasons } \\ \hline \text { 1. } \overline{B A} \cong \overline{B D} ; & \text { 1. Given } \\ \overline{B E} \cong \overline{B C}\end{array} \quad \begin{array}{l}\text { 2. Vertical } \\ \text { Angles } \\ \text { Theorem }\end{array}\right]$

## Reading Strategies

1. Not SAS
2. SAS
3. SAS

## Success for English Learners

1. Since $\triangle K L M$ and $\triangle K N M$ share the side $\overline{K M}$, that side has to be the same. You could then apply SAS to $\overline{L K}, \angle L K M, \overline{K M}$ and $\overline{N K}, \angle N K M, \overline{K M}$.
2. Yes. Separating the triangles would not alter the lengths of the given congruent sides or change any of the angle measures.

## LESSON 5-4

## Practice and Problem Solving: A/B

1. $B D=F H=6$, so $\overline{B D} \cong F H$ by definition of $\cong$ segments. $B C=F G=8$, so $\overline{B C} \cong \overline{F G}$ by definition of $\cong$ segments. $C D=G H=9$, so $\overline{C D} \cong \overline{G H}$ by definition of $\cong$ segments. Therefore, $\triangle B C D \cong \triangle F G H$ by SSS.
2. Possible answer: Since $A B \cong A D$, $3 x-11=x+7$. Solving for $x, x=9$. Substituting the value of $x$ into the expressions gives $A B=A D=16$ and $C B=C D=13$. Finally, $C A=C A$. So, the triangles are congruent by the SSS Congruence Theorem, and $\angle B \cong \angle D$ by CPCTC.
3. Possible answer: No. There are only two pairs of congruent sides between the two triangles ( $\overline{H G} \cong \overline{H J} ; \overline{H K} \cong \overline{H K}$ ), so the triangles are not necessarily congruent. Therefore it cannot be determined whether $\overline{G K} \cong \overline{J K}$, which would have to be true if $\overline{H K}$ is the perpendicular bisector of $\overline{G J}$.
4. 

\(\left.$$
\begin{array}{|l|l|}\hline \text { Statements } & \text { Reasons } \\
\hline \text { 1. } \overline{X Y} \cong \overline{Z Y} & \text { 1. Given } \\
\hline \text { 2. } \overline{X O} \cong \overline{Z O} & \begin{array}{l}\text { 2. Radii of a } \\
\text { circle } \\
\text { are } \\
\text { congruent. }\end{array} \\
\hline \text { 3. } \overline{Y O} \cong \overline{Y O} & \begin{array}{l}\text { 3. Reflexive } \\
\text { property of } \\
\text { congruence }\end{array} \\
\hline \text { 4. } \triangle X Y O \cong & \begin{array}{l}\text { 4. SSS } \\
\triangle Z Y O\end{array}
$$ <br>
Triangle <br>

Theorem\end{array}\right]\)| 5. $\angle X \cong \angle Z$ | 5. CPCTC |
| :---: | :---: |

## Practice and Problem Solving: C

1. We know that $\overline{A K} \cong \overline{B K}$. Since $J$ is the midpoint of $\overline{A B}, \overline{A J} \cong \overline{B J}$ by def. of midpoint. $\overline{J K} \cong \overline{J K}$ by Reflexive Property of $\cong$. So $\triangle A K J \cong \triangle B K J$ by SSS.
2. Yes; possible answer: The diagonal is the hypotenuse of an isosceles right triangle. The length of one side of the square (one leg of the triangle) can be found by using the Pythagorean Theorem, and knowing one side is enough to draw a specific square.
3. 540 sq ft
4. 

| Statements | Reasons |
| :--- | :--- |
| 1. $\overline{A B} \cong \overline{E F} ; \angle B \cong \angle F ;$ | 1. Given |
| $\overline{B C} \cong \overline{F G}$ |  |
| 2. $\triangle A B C \cong \triangle E F G$ | 2. SAS |
| 3. $\overline{A C} \cong \overline{E G}$ and | 3. CPCTC |
| $\angle B C A \cong \angle F G E$ |  |
| 4. $\angle C \cong \angle G$ | 4. Given |
| 5. $\mathrm{m} \angle C=\mathrm{m} \angle B C A+$ | 5. Angle addition |
| $\mathrm{m} \angle A C D$ |  |
| $\mathrm{~m} \angle \mathrm{G}=\mathrm{m} \angle F G E+$ |  |
| $\mathrm{m} \angle E G H$ |  |
| $\mathrm{~m} \angle A C D=\mathrm{m} \angle E G H$ |  |
| 6. $\angle D \cong \angle H$ | 6. Given |
| 7. $\triangle A C D \cong \triangle E F G$ | 7. AAS |


| 8. $\overline{C D} \cong \overline{G H}$ and | 8. CPCTC |
| :--- | :--- |
| $\overline{A D} \cong \overline{E H}$ |  |$\quad$| 9. All |
| :--- |
| corresponding |
| parts are |
| congruent. |$\quad$| 9. $A B C D \cong E F G H$ |
| :--- |

## Practice and Problem Solving:

 Modified1. $\overline{U V}$ and $\overline{X Y} ; \overline{V W}$ and $\overline{Y Z} ; \overline{W U}$ and $\overline{Z X}$
2. $\overline{C A}$ and $\overline{B U} ; \overline{A R}$ and $\overline{U G} ; \overline{R C}$ and $\overline{G B}$
3. $\triangle T U V \cong \triangle W X Y$
4. $\triangle J K M \cong \triangle L K M$
5. $\triangle A B C \cong \triangle C D A$
6. $\triangle I F A \cong \triangle G F H$
7. | Statements | Reasons |
| :---: | :---: |
| 1. $\overline{W X} \cong \overline{Y X}$ | 1. Given |
| 2. $\overline{W Z} \cong \overline{Y Z}$ | 2. Definition of bisector |
| 3. $\overline{X Z} \cong \overline{X Z}$ | 3. Reflexive Property of <br> Congruence |
| 4. $\Delta W X Z \cong$ <br> $\Delta Y X Z$ | 4. SSS Triangle <br> Theorem |
| 5. $\angle W \cong \angle Y$ | 5. Congruent parts of <br> congruent triangles <br> are congruent. |

## Reading Strategies

1. Both compare sides of two triangles.
2. SAS compares both angles and sides of two triangles, while SSS compares only sides.
3. Yes
4. No
5. No
6. No

## Success for English Learners

1. Yes, as long as the quadrilateral is a parallelogram. If it is not a parallelogram, then no.
2. Yes. The measures of the angles and the lengths of the sides are related.
